



Informatics



## **Seminari i parë shkencorë i Fakultetit të Inxhinierisë Elektrike dhe Kompjuterike**

Artificial Intelligence and Optimization for Automated  
Planning and Scheduling

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Christian Doppler Laboratory for Artificial Intelligence and  
Optimization for Planning and Scheduling  
Database and Artificial Intelligence Group

TU Wien

# Research in Christian Doppler Laboratories



Application-orientated basic research

Cooperation between science and business

“A research group elaborates fundamental knowledge that flows into the development of new products and processes at commercial partners”

# Industrial Partners



- Leading global supplier of technology and services



- Its core expertise is capacity and production planning and scheduling
- Rich expertise in heuristics

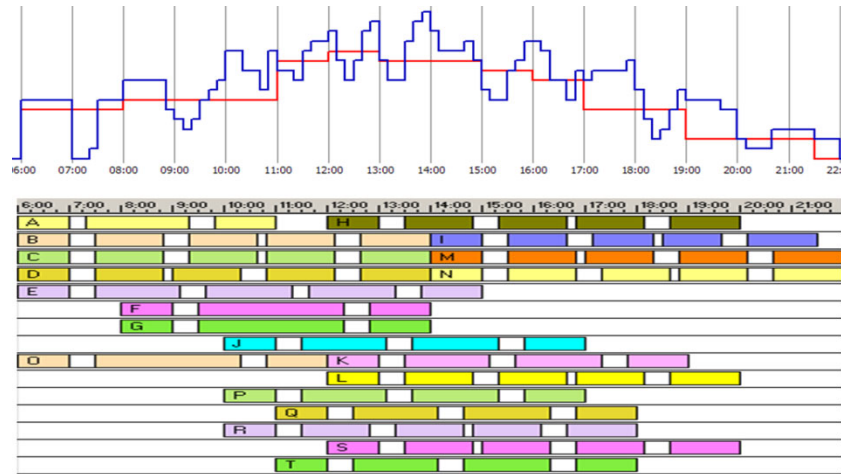


- It offers software and consulting services for workforce/working hours issues
- Spin-off of the TU Wien

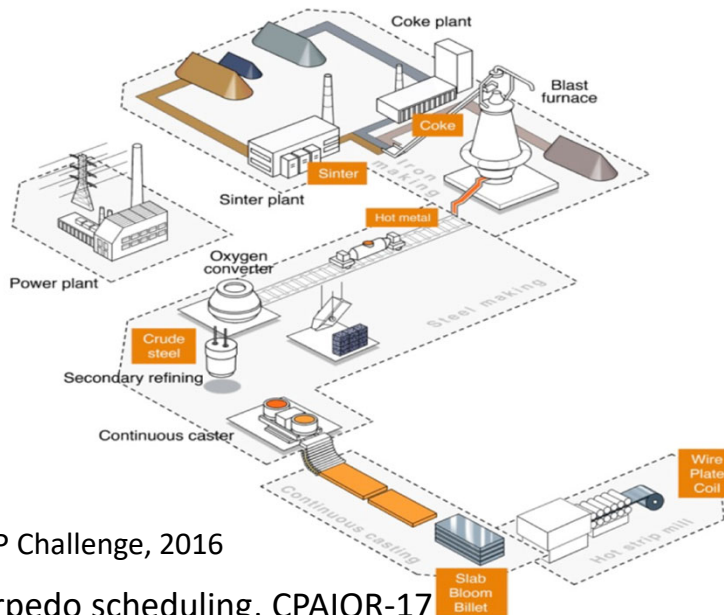
# Planning and Scheduling Problems

|   | Mo | Di | Mi | Do | Fr | Sa | So |
|---|----|----|----|----|----|----|----|
| A | F  | F  | F  | S  | S  |    |    |
| B |    | N  | N  | N  | N  |    |    |
| C |    | F  | F  | N  | N  | N  | N  |
| D |    |    | S  | S  | S  | N  | N  |
| E | N  |    |    | F  | F  | S  | S  |
| F | S  |    |    | F  | F  | F  | F  |
| G | S  | S  |    |    |    | F  | F  |
| H | F  | S  | S  |    |    | S  | S  |
| I | N  | N  | N  |    |    |    |    |

Personnel scheduling, IJCAI-17



Break scheduling, IEEE Intelligent Systems (2010)



ACP Challenge, 2016

Torpedo scheduling, CPAIOR-17

More examples in health care, production, education, public transport, ...

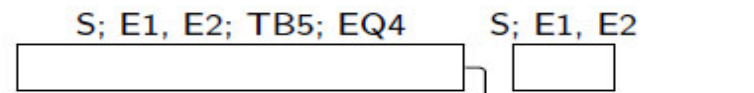
**Very important problems**

Their solutions impact people's everyday life and the efficiency of operations

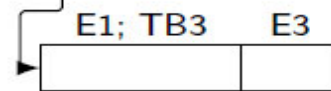
# Task Scheduling/Project Scheduling/Test Laboratory Scheduling

## Project 1

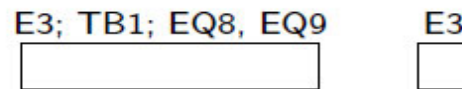
Job 1  
(Tasks 1, 2, 3, 5)



Job 2  
(Task 4)

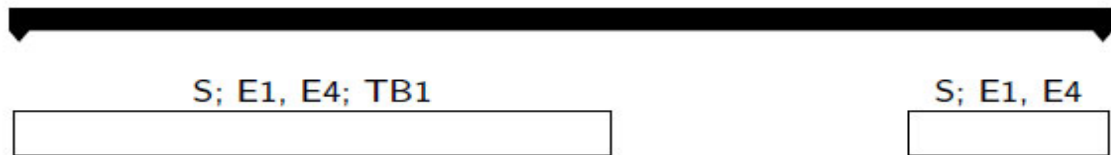


Job 3  
(Tasks 6, 7)

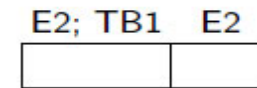


## Project 2

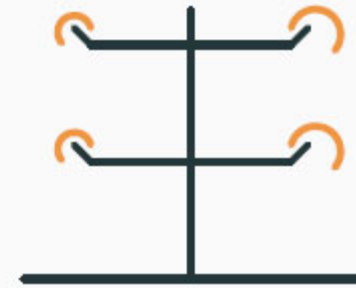
Job 4  
(Tasks 8, 9, 10, 11)



Job 5  
(Task 12)

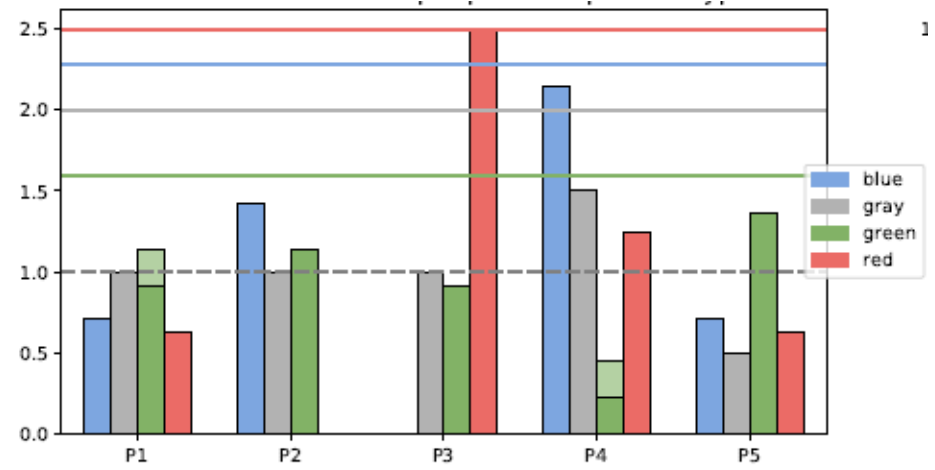
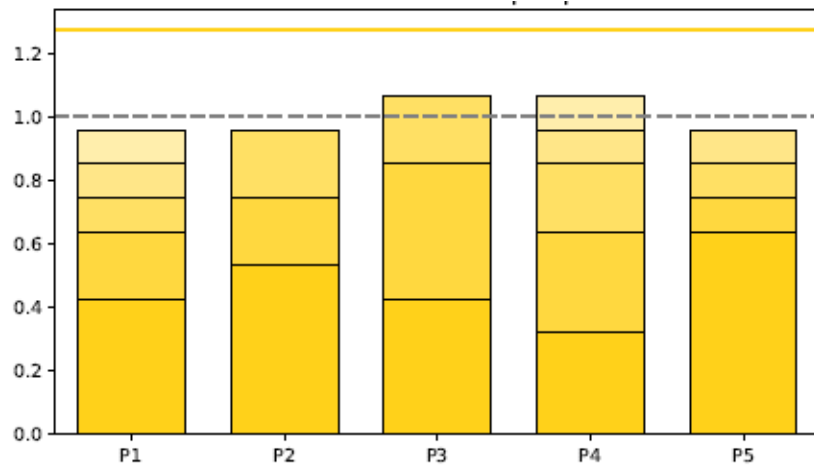


# Automotive Paint Shop Scheduling Problem

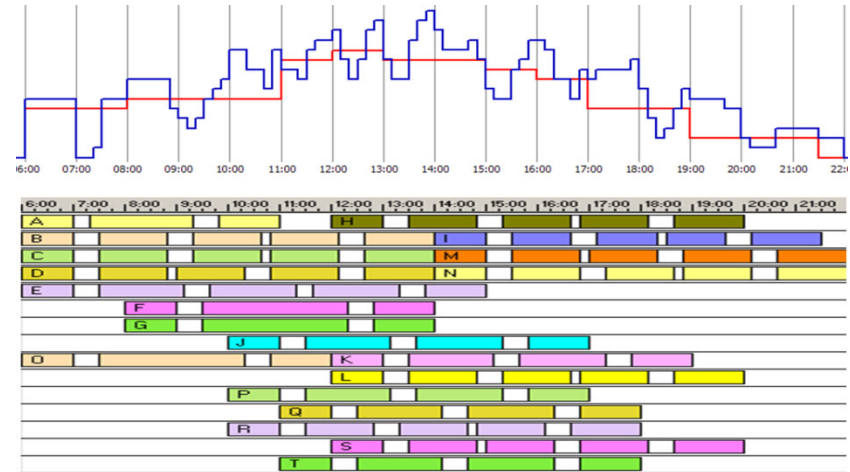
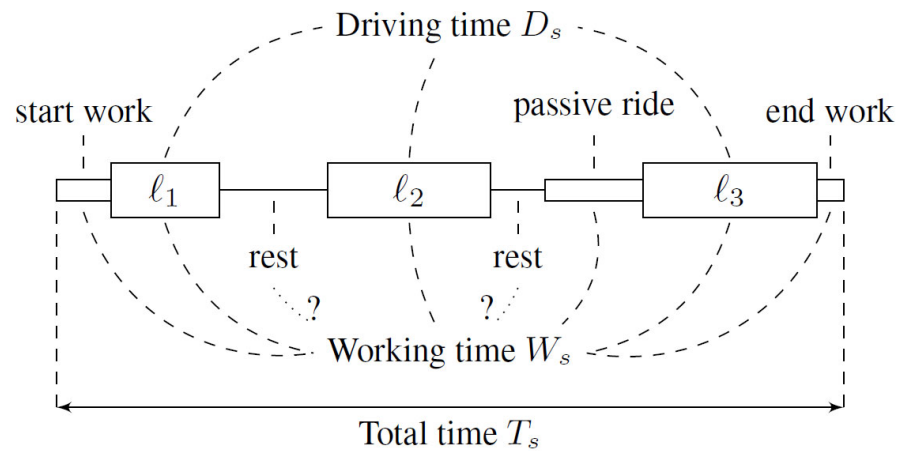


|   | <i>R1</i> | <i>R2</i> | <i>R3</i> | ... |
|---|-----------|-----------|-----------|-----|
| 1 | ↓ A       | A         | C         | ... |
| 2 | A         | A         | C         | ... |
| 3 | A         | C         | C         | ... |
| 4 | B         | B         | B         | ... |
| 5 | B         | B         | B         | ... |

# Production Leveling Problem



# Personnel Planning and Scheduling

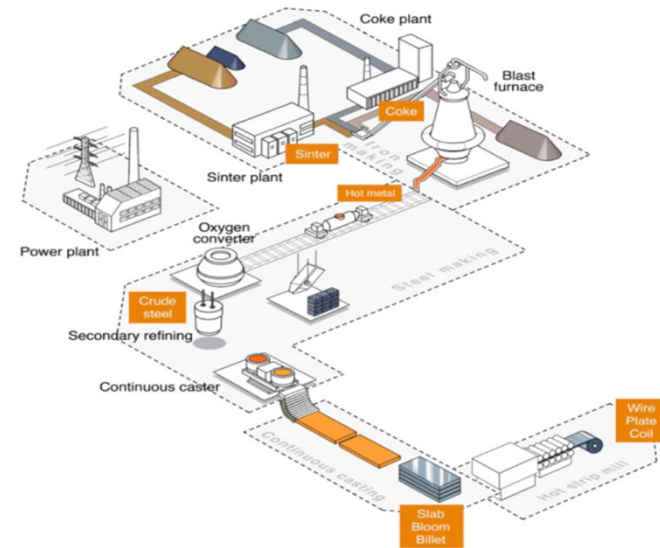


|   | Mo       | Di       | Mi       | Do       | Fr       | Sa       | So       |
|---|----------|----------|----------|----------|----------|----------|----------|
| A | F        | F        | F        | S        | S        |          |          |
| B |          | <b>N</b> | <b>N</b> | <b>N</b> | <b>N</b> |          |          |
| C |          | F        | F        | <b>N</b> | <b>N</b> | <b>N</b> | <b>N</b> |
| D |          |          | S        | S        | S        | <b>N</b> | <b>N</b> |
| E | <b>N</b> |          |          | F        | F        | S        | S        |
| F | S        |          |          | F        | F        | F        | F        |
| G | S        | S        |          |          |          | F        | F        |
| H | F        | S        | S        |          |          | S        | S        |
| I | <b>N</b> | <b>N</b> | <b>N</b> |          |          |          |          |



# Other real-life problems

Torpedo Scheduling Problem

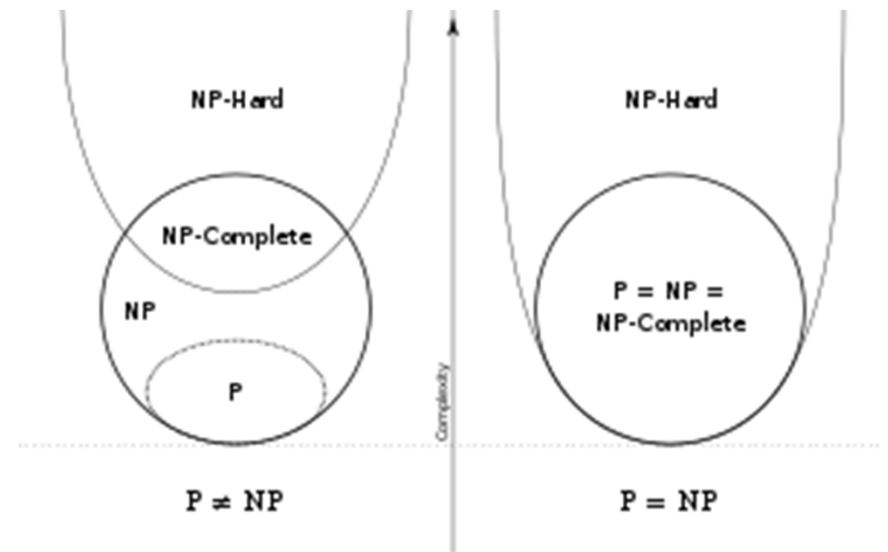


Parallel Machine Scheduling

Curriculum-based Course Timetabling

# The General Obstacle

- NP-hard (intractable) problems
- No efficient algorithms could be found yet
- P problems can be solved efficiently (in polynomial time)
- $P \neq NP$  ? (**Millennium Prize Problem**)



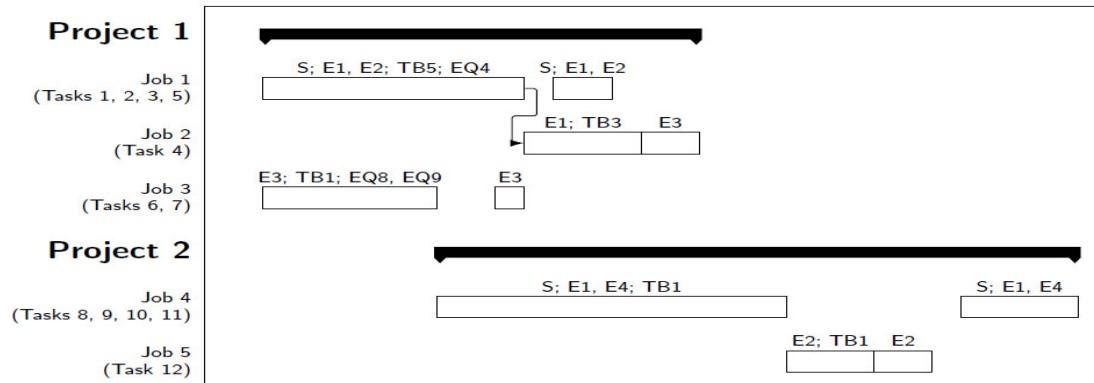
<https://en.wikipedia.org/wiki/NP-hardness>

**Tremendous size of the search space  
of possible candidate solutions**

# Search Space

|   | Mo       | Di       | Mi       | Do       | Fr       | Sa       | So       |
|---|----------|----------|----------|----------|----------|----------|----------|
| A | F        | F        | F        | S        | S        |          |          |
| B |          | <b>N</b> | <b>N</b> | <b>N</b> | <b>N</b> |          |          |
| C |          | F        | F        | <b>N</b> | <b>N</b> | <b>N</b> | <b>N</b> |
| D |          |          | S        | S        | S        | <b>N</b> | <b>N</b> |
| E | <b>N</b> |          |          | F        | F        | S        | S        |
| F | S        |          |          | F        | F        | F        | F        |
| G | S        | S        |          |          |          | F        | F        |
| H | F        | S        | S        |          |          | S        | S        |
| I | <b>N</b> | <b>N</b> | <b>N</b> |          |          |          |          |

$10^{84}$



$10^{3000}$

# State-of-the-art methods

## Complete approaches

Mathematical programming  
Constraint programming  
Answer set programming  
SAT/SMT

...

**Solvers and constraint languages:** IBM (CPLEX, CP Optimizer), Gurobi, Google (OR-Tools), Chuffed, MiniZinc ...

## Metaheuristics

Tabu Search  
Simulated Annealing  
Evolutionary Strategies  
Memetic Algorithms

...

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...



- Domain specific solutions
- For many problems optimal solutions are not known
- New challenging problems that cannot be optimally solved (e.g., problems from our industrial partners)

# State-of-the-art methods

## Complete approaches

Mathematical programming  
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SAT/SMT

...

## Solvers

Google

## Metaheuristics

Tabu Search  
Simulated Annealing  
Evolutionary Strategies  
Memetic Algorithms

...

Gurobi,

**New algorithms/techniques needed**



- Domain specific solutions
- For many problems optimal solutions are not known
- New challenging problems that cannot be optimally solved (e.g., problems from our industrial partners)

# Goals and Methods

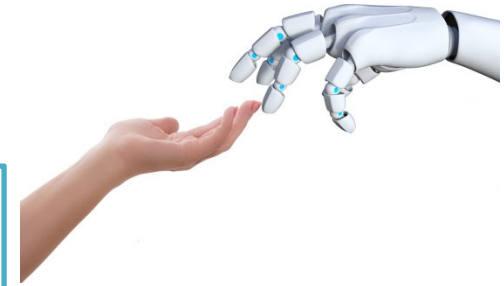
**Overall goal:** New generation of planning and scheduling algorithms

- Scalable in practice
- Domain independent
- Online adaptive

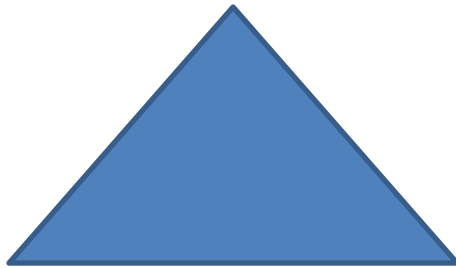
## **Methods**

- Novel modeling approaches for state-of-the art solvers
- Hybrid techniques
- Machine learning and automated algorithm selection
- Automated algorithm design

# Hybrid Algorithms



*Methods of Artificial Intelligence  
(Machine Learning...)*



*Methods of Logic*

*Mathematical Optimization*

$$S_{i,d,t} \Leftrightarrow \bigwedge_{x=1}^{sl_t} U_{i,d,x} \bigwedge_{y=sl_t}^{sl_{max}} \neg U_{i,d,y}$$

$$\begin{aligned} \text{minimize } f = & 30 * \sum_{\substack{s \in S \\ k \in K \\ d \in \{1 \dots 7\}}} C_{skd}^{S1} \\ & + 15 * \sum_{\substack{n \in N \\ s \in S \\ d \in \{1 \dots 7\}}} (C_{nsd}^{S2a} + C_{nsd}^{S2b}) \\ & + 30 * \sum_{\substack{n \in N \\ d \in \{1 \dots 7\}}} (C_{nd}^{S2c} + C_{nd}^{S2d}) \end{aligned}$$



# Parallel Machine Scheduling

minimise  $Lex(\Sigma_{j \in J}(T_j), C_{max})$ , subject to

$$\Sigma_{m \in M}(Y_{j,m}) = 1, \forall j \in J$$

$$\Sigma_{i \in J_0, i \neq j}(X_{i,j,m}) = Y_{j,m}, \forall j \in J, m \in M$$

$$\Sigma_{j \in J_0, i \neq j}(X_{i,j,m}) = Y_{i,m}, \forall i \in J, m \in M$$

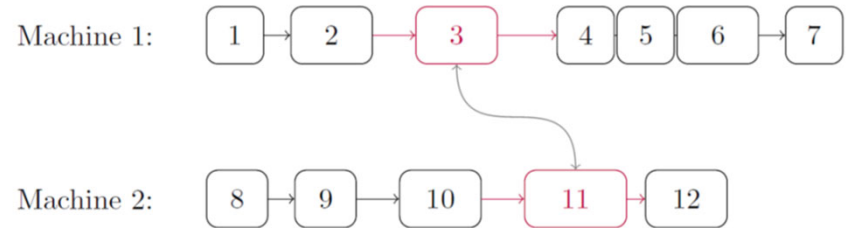
$$C_j \geq C_i + s_{i,j,m} + p_{j,m} + V \cdot (X_{i,j,m} - 1), \\ \forall i \in J_0, j \in J, m \in M$$

$$\Sigma_{j \in J}(X_{0,j,m}) \leq 1, \forall m \in M$$

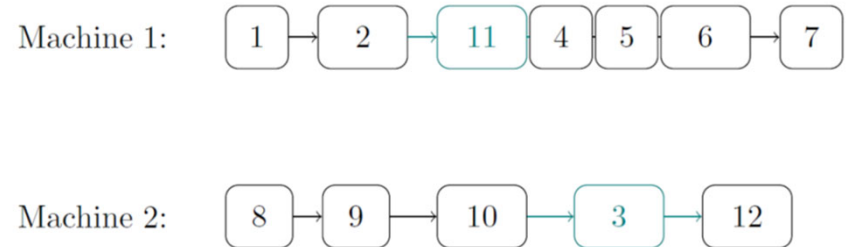
$$\Sigma_{i \in J_0, j \in J, i \neq j}(s_{i,j,m} \cdot X_{i,j,m}) + \\ \Sigma_{i \in J}(p_{i,m} \cdot Y_{i,m} + s_{i,0,m} \cdot X_{i,0,m}) \leq C_{max}, \\ \forall m \in M$$

$$T_j \geq C_j - d_j, \forall j \in J$$

$$T_j \geq 0, \forall j \in J$$



(a) Before Move Application



(b) After Move Application

# Test Laboratory Scheduling

$$\xi(\xi(a)) = \xi(a) \quad a \in A^* \quad (1)$$

$$p_a = p_{\xi(a)} \wedge f_a = f_{\xi(a)} \quad a \in A^* \quad (2)$$

$$\text{all\_equal}(\{\xi(a) \mid a \in \dot{A}_j^F\}) \quad j \in J^0 \quad (3)$$

$$\xi(a) \leq a \quad a \in A^* \quad (4)$$

$$s_{\xi(a)} \geq \alpha_a \wedge n_{\xi(a)} \leq \omega_a \quad a \in A^* \quad (5)$$

$$d_a = n_a - s_a \quad a \in J \quad (6)$$

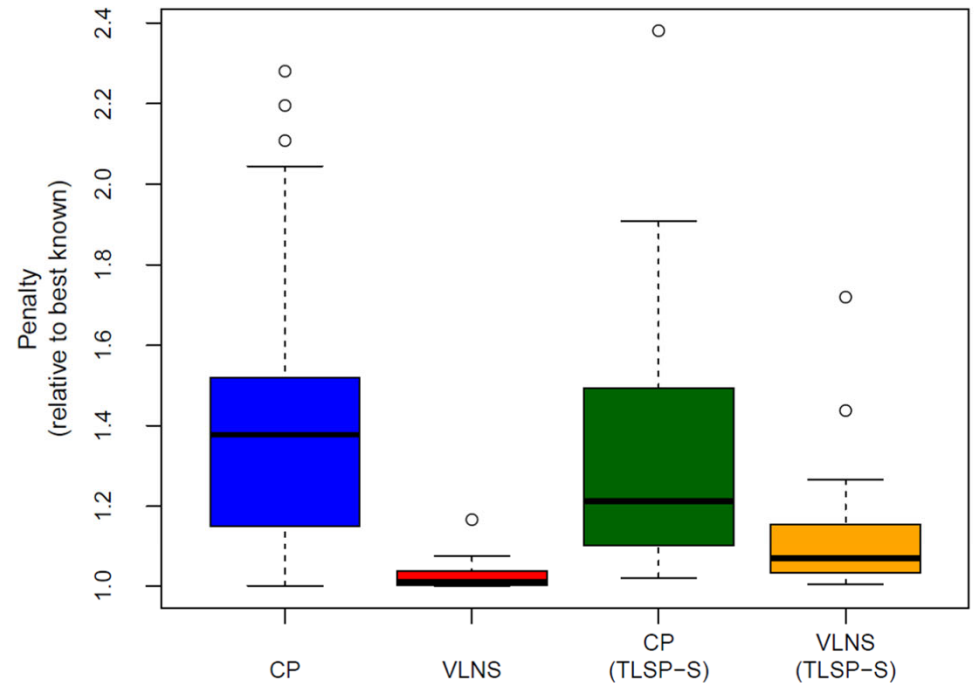
$$d_a \cdot \mathcal{M} \geq \sum_{\substack{a' \in A^* \\ \text{s.t. } \xi(a')=a}} d_{a'm_a} + st(a) \quad a \in J \quad (7)$$

$$(d_a - 1) \cdot \mathcal{M} < \sum_{\substack{a' \in A^* \\ \text{s.t. } \xi(a')=a}} d_{a'm_a} + st(a) \quad a \in J \quad (8)$$

$$\xi(a) = \xi(a') \vee n_{\xi(a')} \leq s_{\xi(a)} \quad a \in A^*, a' \in \mathcal{P}_a \quad (9)$$

$$s_{\xi(a)} = 1 \quad j \in J^{0S}, a \in \dot{A}_j \quad (10)$$

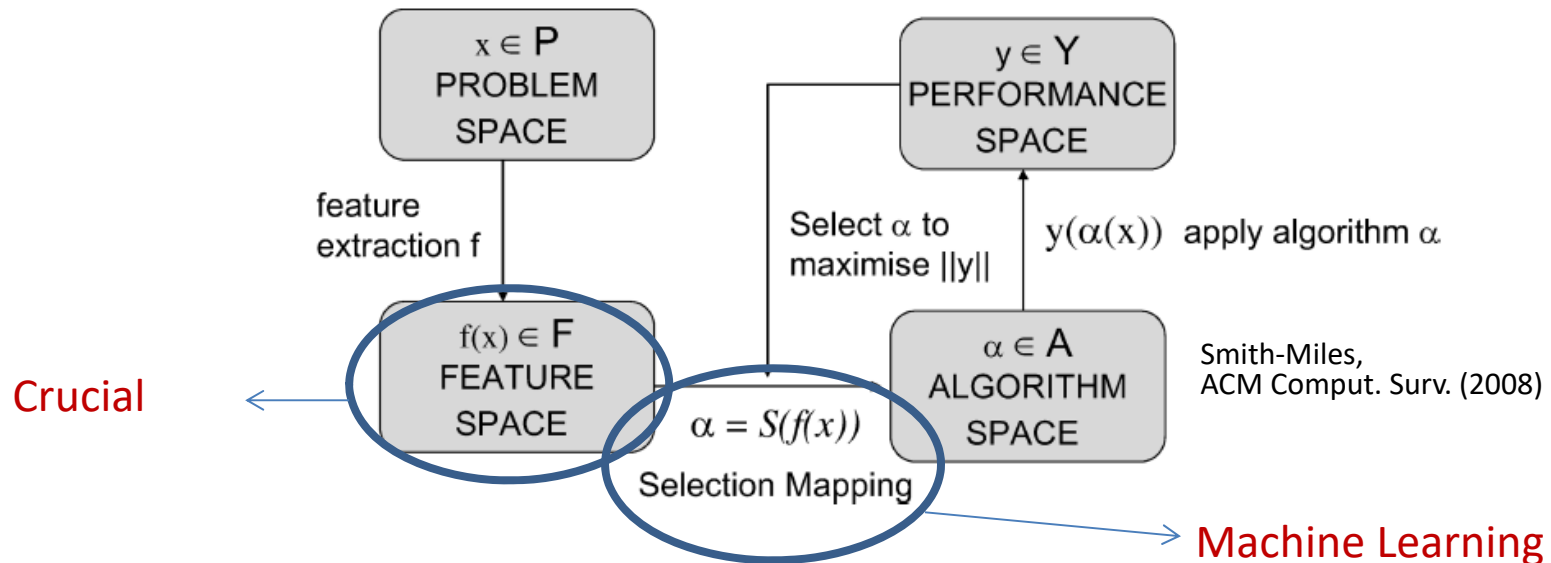
$$\text{cumulative}((s_a)_{a \in A^*}, (d_{m_a a})_{a \in A^*}, (a_{ea}^{Em})_{a \in A^*}, 1) \quad e \in E \quad (11)$$



# Automated Algorithm Selection

## No free lunch theorem

“...for any algorithm, any elevated performance over one class of problems is offset by performance over another class” (Wolpert & Macready, IEEE Trans. Evo. Comp., 1997)

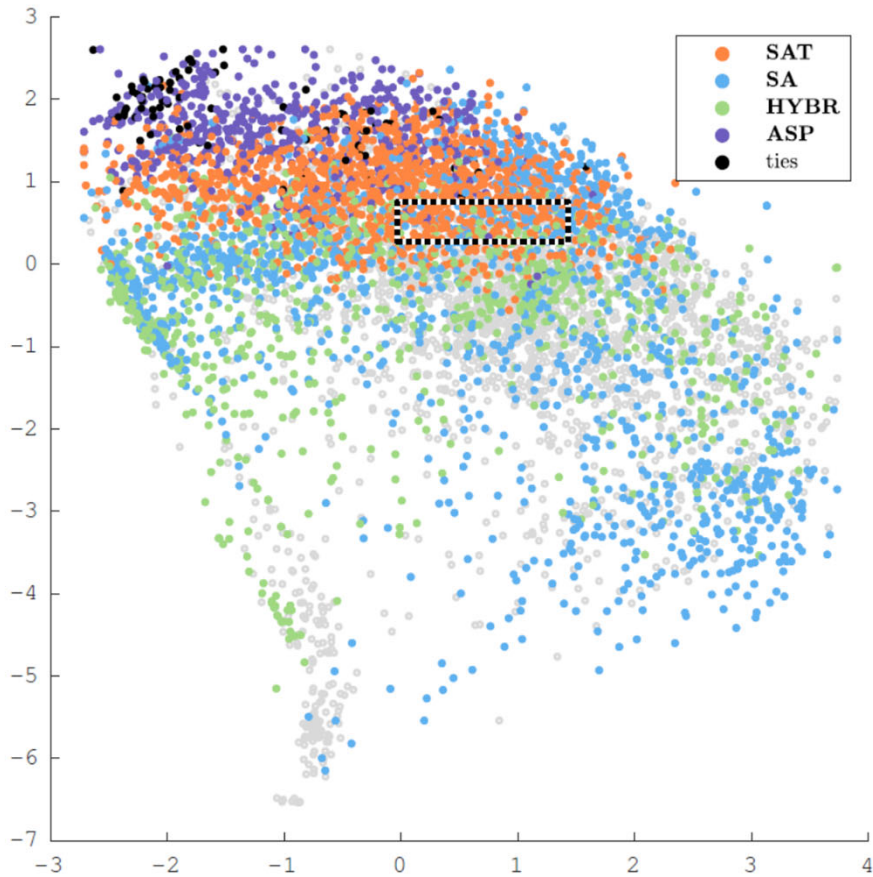


## Success Stories

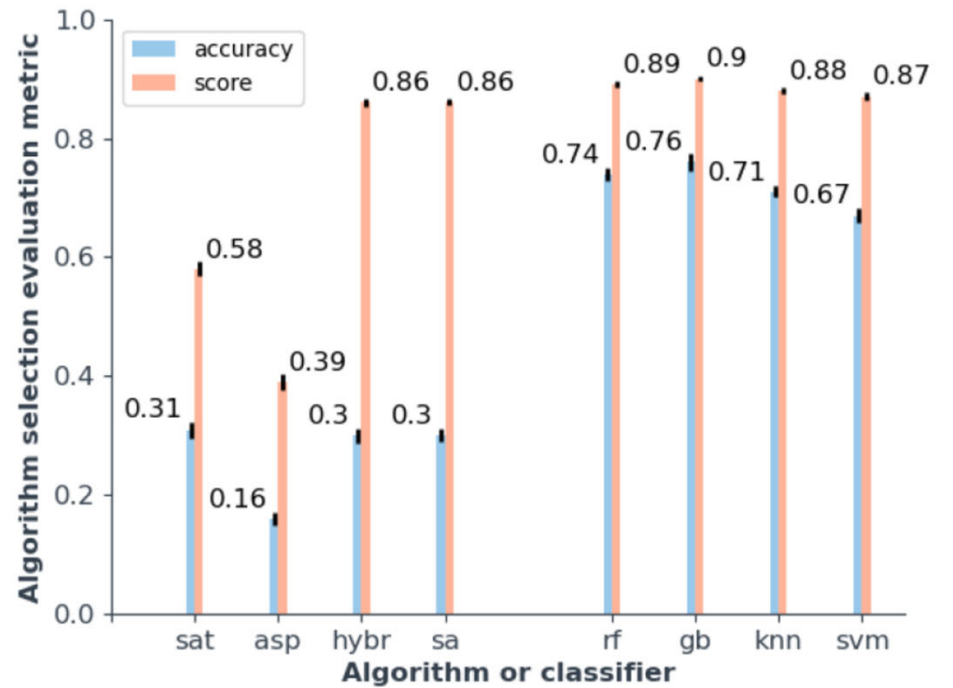
SAT, TSP, Graph Coloring, Combinatorial Auctions,...

**⚠ Problem specific features**

# Curriculum-based Course Timetabling



(b) Best performance (with time)



# Personnel Scheduling

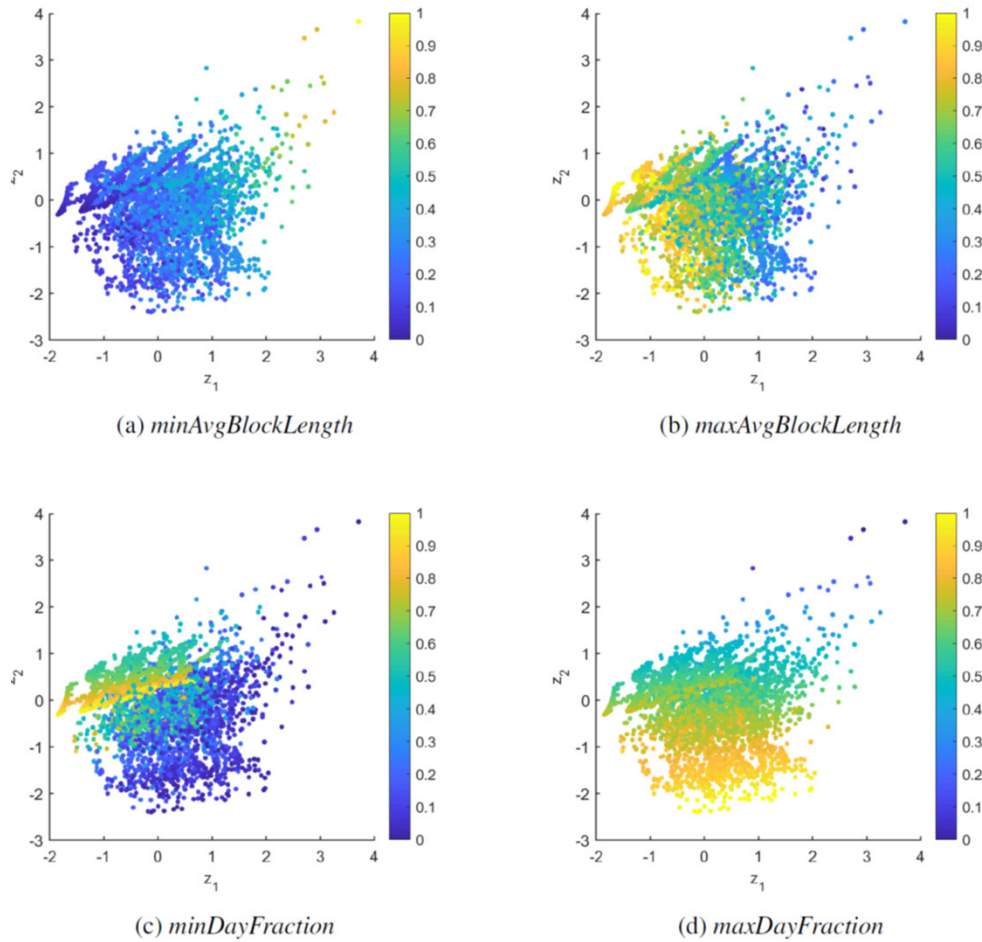


Fig. 5: Selected features for the extended instance set

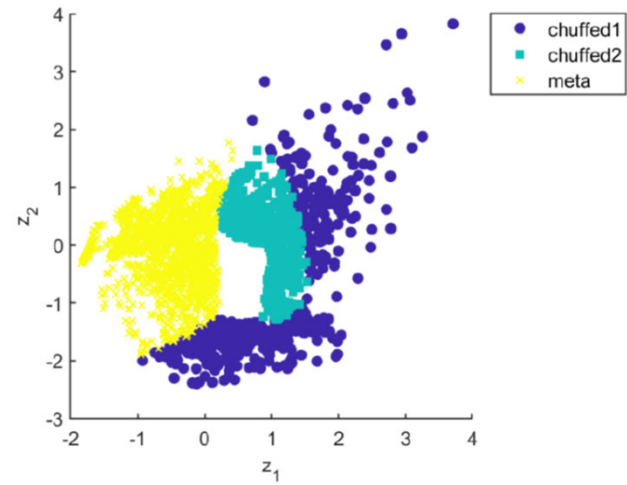
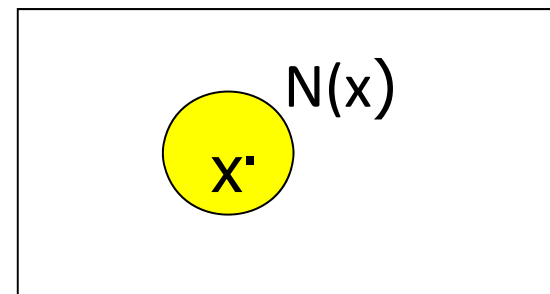
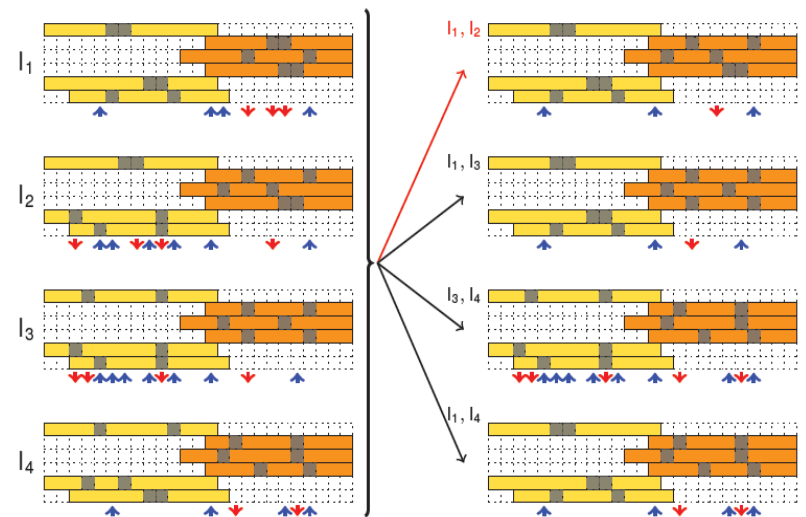
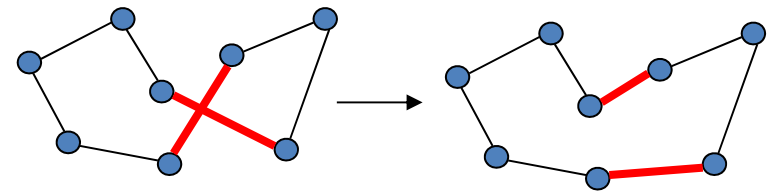


Fig. 9: Algorithm portfolio

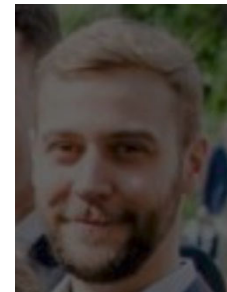
# Future Work: Automated Algorithm Design

Automated generation of low-level heuristics and operators

Algorithm design by hyper-heuristics



# CD-Laboratory: Researchers



## CPAIOR 2021

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18th International Conference on the Integration of Constraint Programming, Artificial Intelligence, and Operations Research, July 5-8, 2021, Vienna, Austria.

Program Chair: Peter Stuckey  
Conference Chair: Nysret Musliu

[CONFERENCE WEBSITE](#)



# Selected References

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- Tobias Geibinger, Florian Mischek, Nysret Musliu. Constraint Logic Programming for Real-World Test Laboratory Scheduling. ***The Thirty-Fifth AAAI Conference on Artificial Intelligence (AAAI-21)***.
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- *Johannes Vass, Marie-Louise Lackner, Christoph Mrkvicka, NysretMusliu, Felix Winter. Exact and Meta-Heuristic Approaches for the Production Leveling Problem. Submitted to Journal of Scheduling.*
- *Arnaud De Coster , Nysret Musliu, Andrea Schaerf, Johannes Schoisswohl, Kate Smith-Miles. Algorithm Selection & Instance Space Analysis for Curriculum-based Course Timetabling. Submitted to Journal of Scheduling.*

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